

Bergische Universität Wuppertal



Calculation of atmospheric Neutrino- and Myonfluxes with respect to Cosmic Ray Composition

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Content

Goal / Motivation: Determine atmospheric ν – and μ - fluxes.
-> Calibration / Background for μ - / ν - Telescopes using KASCADE-data

1. Basics
2. Input data / What I am doing
3. Unfolding based on QGSJet and SIBYLL
4. Fit strategy
5. Summary & Outlook



1. Basics

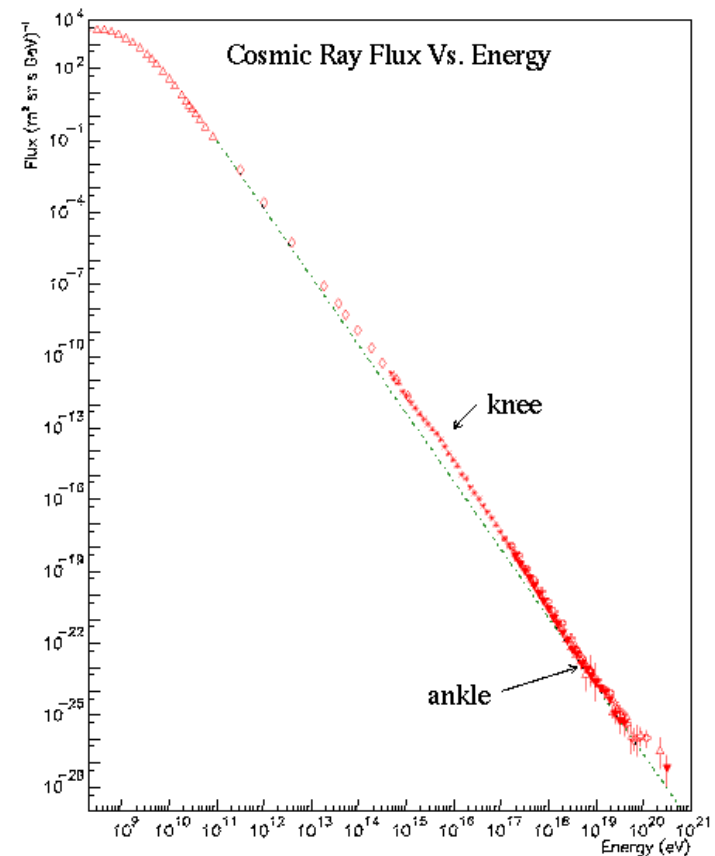
- Energy range of the knee $\sim 4 * 10^{15}$ eV
- $\gamma_1 = 2,7$ for $E < 4 * 10^{15}$ eV
- $\gamma_2 = 3$ for $4 * 10^{15}$ eV $< E < 5 * 10^{18}$ eV
- Further γ 's doesn't play a role here

$$\bullet \frac{dJ}{dE} = c * E^{-\gamma}, \quad c = \text{constant}$$

(c is a „fluxparameter“)

• „Knee“ is a consequence of the „steepening“ of the spectra of light elements (evidence follows)

$$\bullet \text{Assumption : } E_{knee}(Z_X) = Z_X * E_{knee}(p)$$



2. Input data

- KASCADE measures Electron- and Myonnumbers.

- $$X^{measured} = M * \frac{dJ^{true}}{dE}$$

- M includes propagation, properties of detectors...
- Data is unfolded by using two high energetic interaction models (QGSJet , SIBYLL)
-> see KASCADE paper in addition
- Models differ in their predictions about interactions.

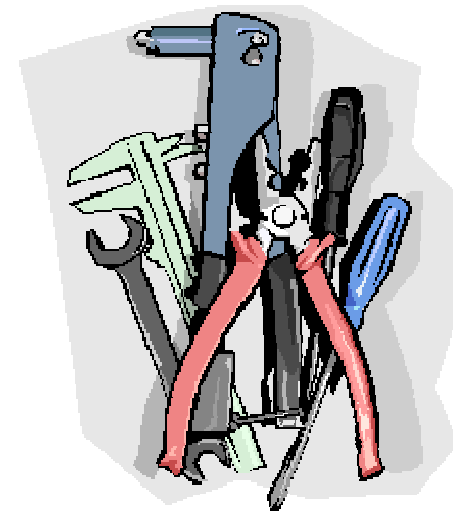
➡ Energy spectra for five representative mass groups (p, He , C, Si, Fe) are reconstructed.

- „Knee region“ is in energy window of KASCADE data.



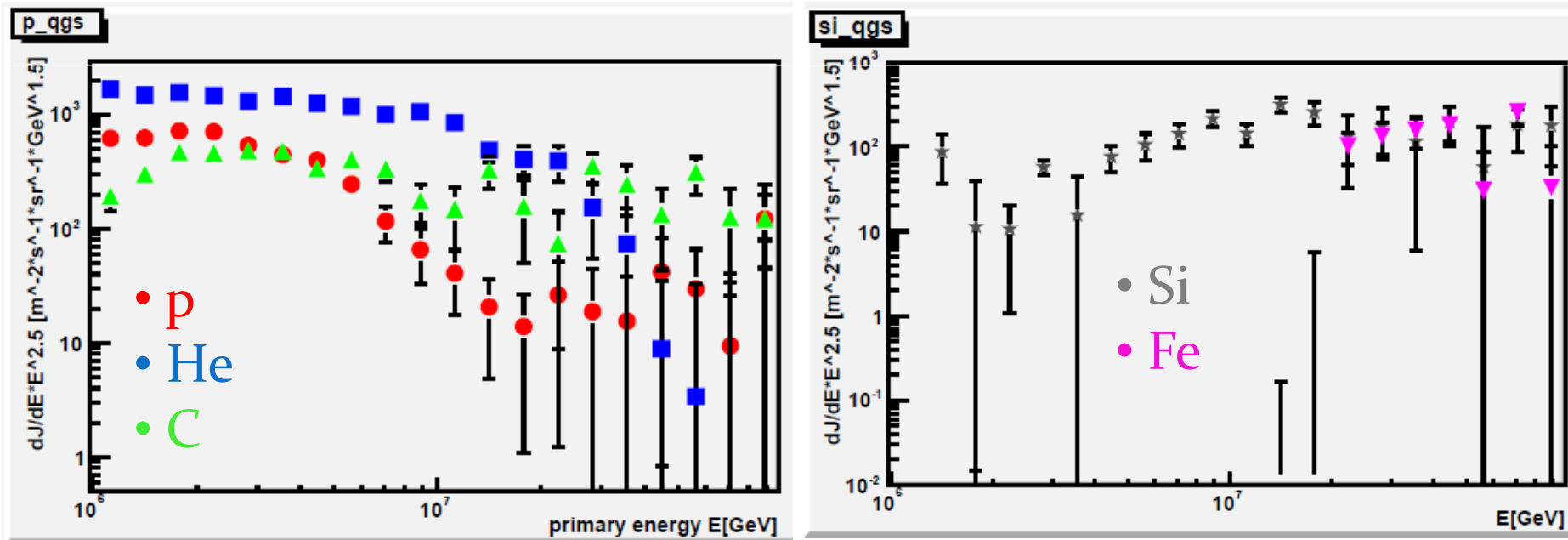
2. What I am doing

- Spectra for each model have to be fitted „simultaneously“ for all element groups.
- Results of the simultaneous fit provides eight parameters :
 - p_1 : Knee position
 - p_2 : Spectral index below the knee
 - p_3 : Spectral index above the knee
 - $p_4 - p_8$: Fluxparameter for each mass group
- Use $p_1 - p_8$
- Weight CORSIKA – shower according to fitparameters $p_1 - p_8$
 - ➔ Predictions for μ - and ν - Fluxes.
- How dependent are the desired fluxes from details of the spectra of the mass groups for each model?



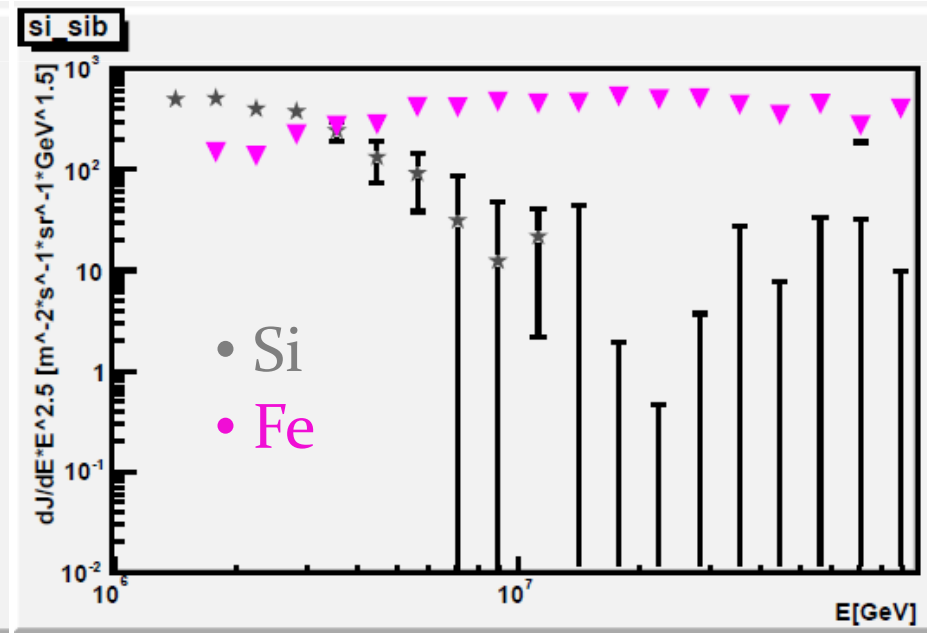
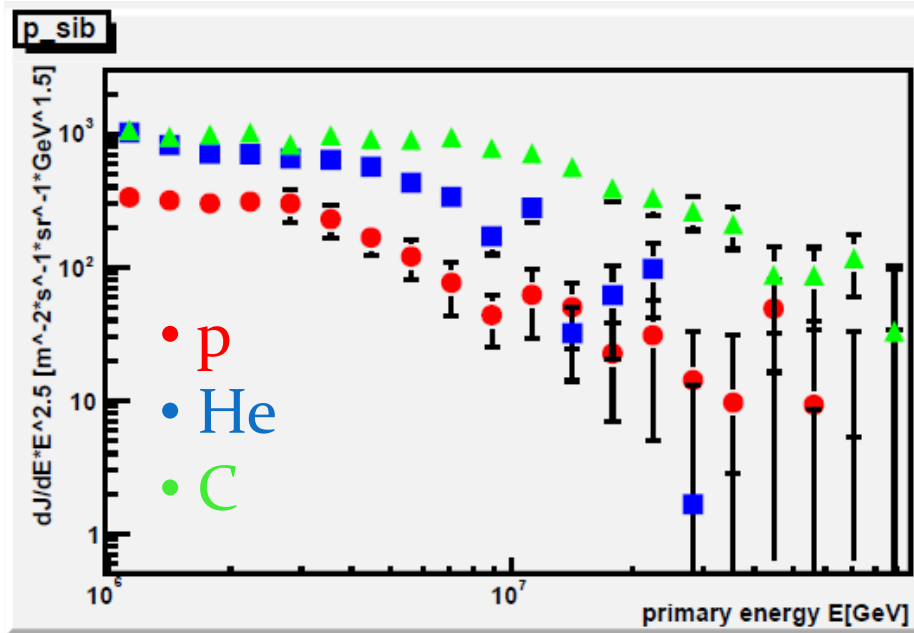
3. Unfolding (QGSJet)

- Unfolded KASCADE data using QGSJet



3. Unfolding (SIBYLL)

- Unfolded KASCADE data using SIBYLL



4. Fit strategies

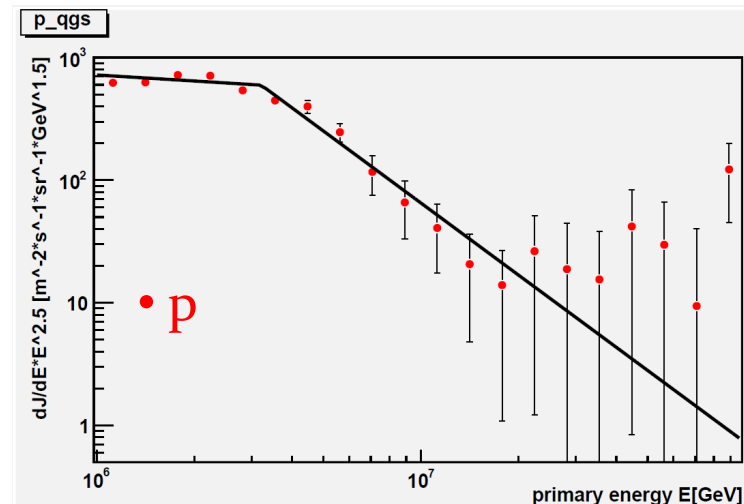
- Parametrisation of the fit (Example for Protons: non-simultaneous fit):

- $\frac{dJ}{dE_{left}} = a * E^{\gamma_1}$ $\frac{dJ}{dE_{right}} = b * E^{\gamma_2}$ (broken power law)

- Continuity: $E = E_{knee} \rightarrow \frac{dJ}{dE_{left}} = \frac{dJ}{dE_{right}} \rightarrow b = a * E_{knee}^{\gamma_1 - \gamma_2}$

➔ $\frac{dJ}{dE_{left}} = a * E^{\gamma_1}$

$$\frac{dJ}{dE_{right}} = a * E_{knee}^{\gamma_1 - \gamma_2} * E^{\gamma_2}$$



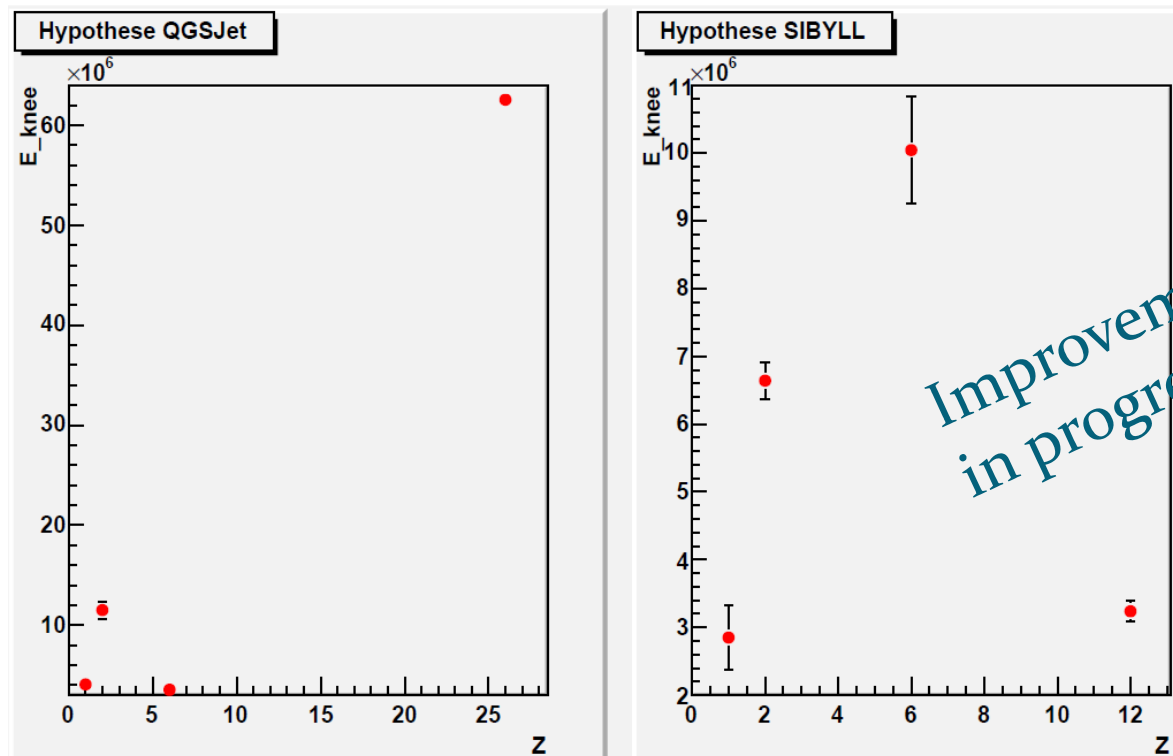
4. Fit strategies

Test of hypothesis:

$$E_{knee}(X) = Z * E_{knee}(p)$$

➔ Plot E_{knee} against Z to test hypothesis.

- Knee energies received by fitting spectra independent from each other. Improvement is in progress!



4. Fit strategies

- Simultaneous fit has the following structure :

[1] = Knee position

[2],[3] = spectral indices below and above the knee

[0],[4],[5],[6],[7] = fluxparameters of the different mass groups

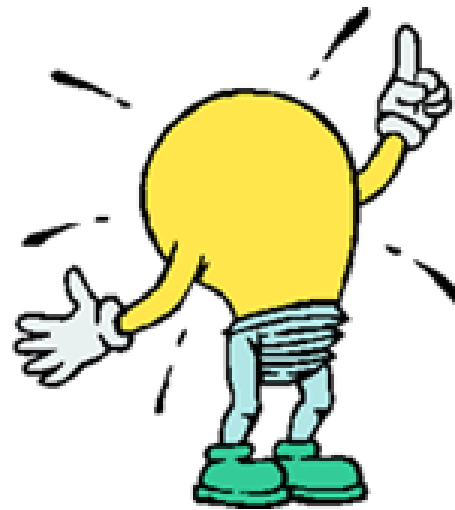
[0][$Z_P * 1$][2][3]

[4][$Z_{He} * 1$][2][3]

[5][$Z_C * 1$][2][3]

[6][$Z_{Si} * 1$][2][3]

[7][$Z_{Fe} * 1$][2][3]



- Assumption = Spectral indices are the same constants for all mass groups.

4. Fit strategies

Fit Method : Minuit

- Concept of Minuit is to write χ^2 by yourself.
- χ^2 depends on data points , errors and free parameters.
- χ^2 can be minimized by several algorithms („MIGRAD“ is used here).

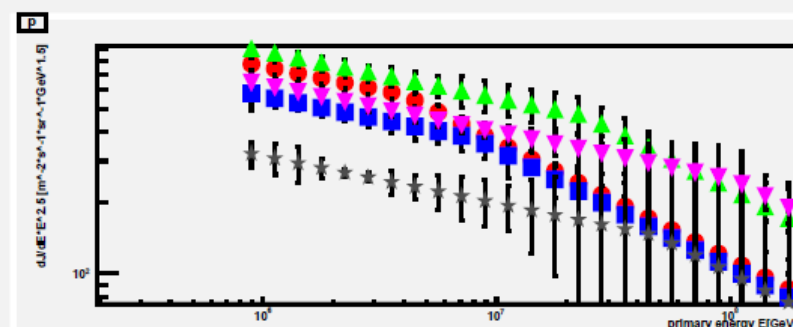
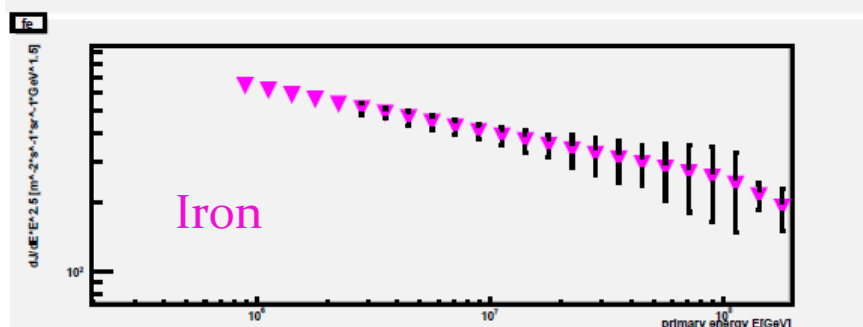
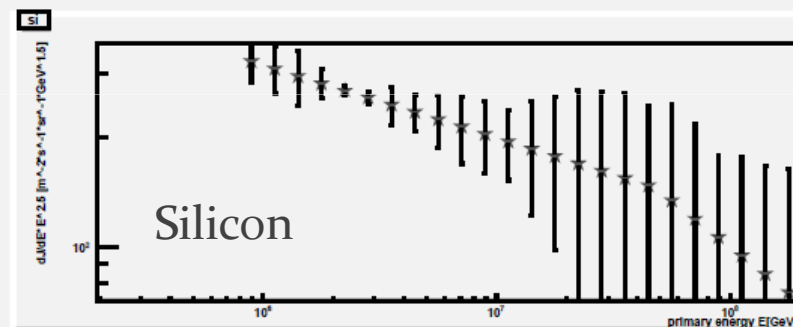
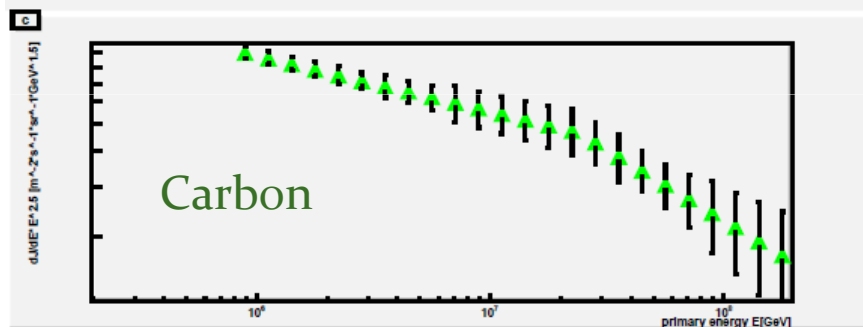
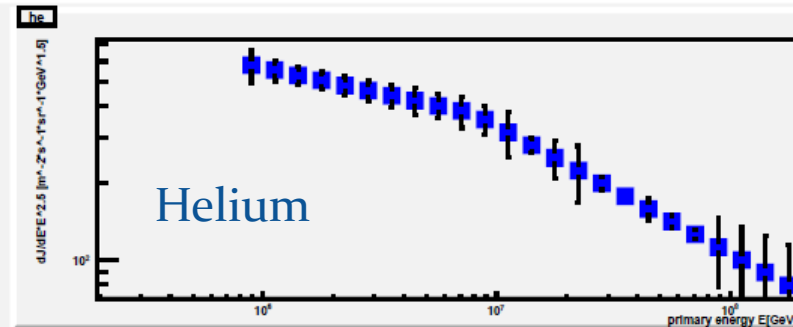
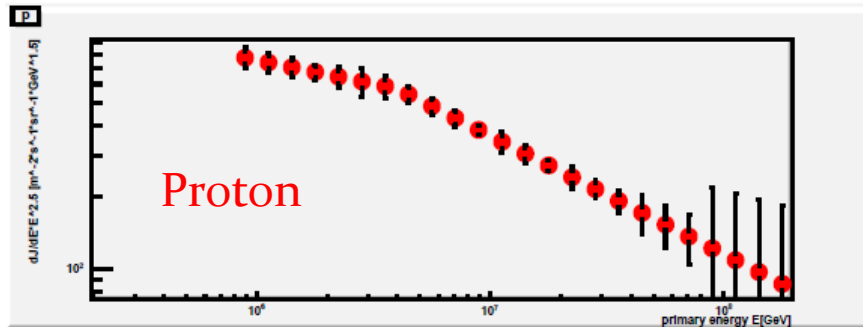
- Final Parameters (QGSJet):
 - [1] = $1,69017 \cdot 10^6 \text{ GeV} \pm 8,16605 \cdot 10^7 \text{ GeV}$
 - [2] = $-4,97137 \pm 4,81064$
 - [3] = $-2,03364 \pm 3,30407$

- Final Parameters(SIBYLL):
 - [1] = $1,12248 \cdot 10^6 \text{ GeV} \pm 1,66706 \text{ GeV}$
 - [2] = $-0,652245 \pm 0,00393992$
 - [3] = $-0,958628 \pm 0,0117727$

- Are the parameters meaningful? Is the used Method meaningful?

4. Fit strategies

Test of procedure : Roll the dice!

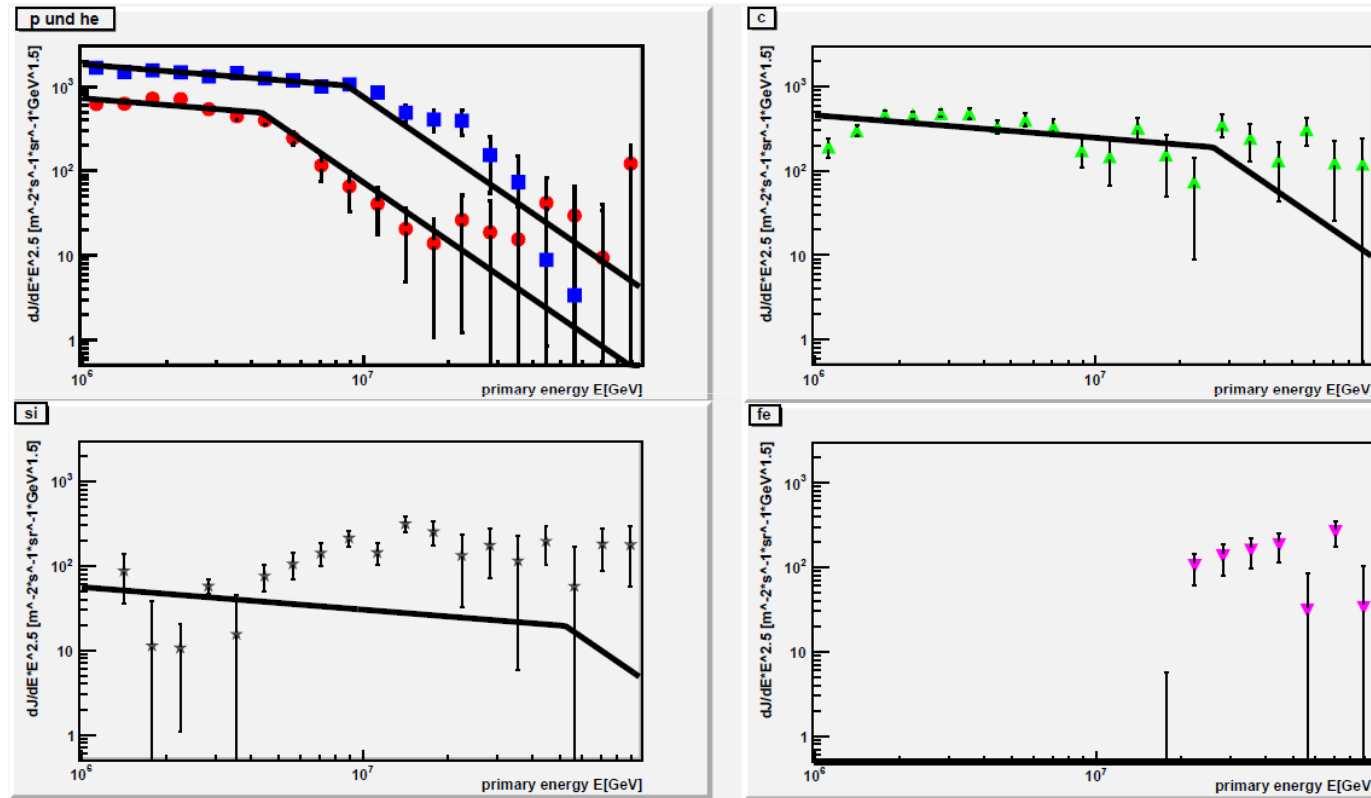


- First test successful , but must be improved!

4. Fit strategies

Improved fit with Minuit : Use iterations

QGSJet



$$[1] = 4.35895e+06 \text{ GeV} \pm 126266 \text{ GeV}$$

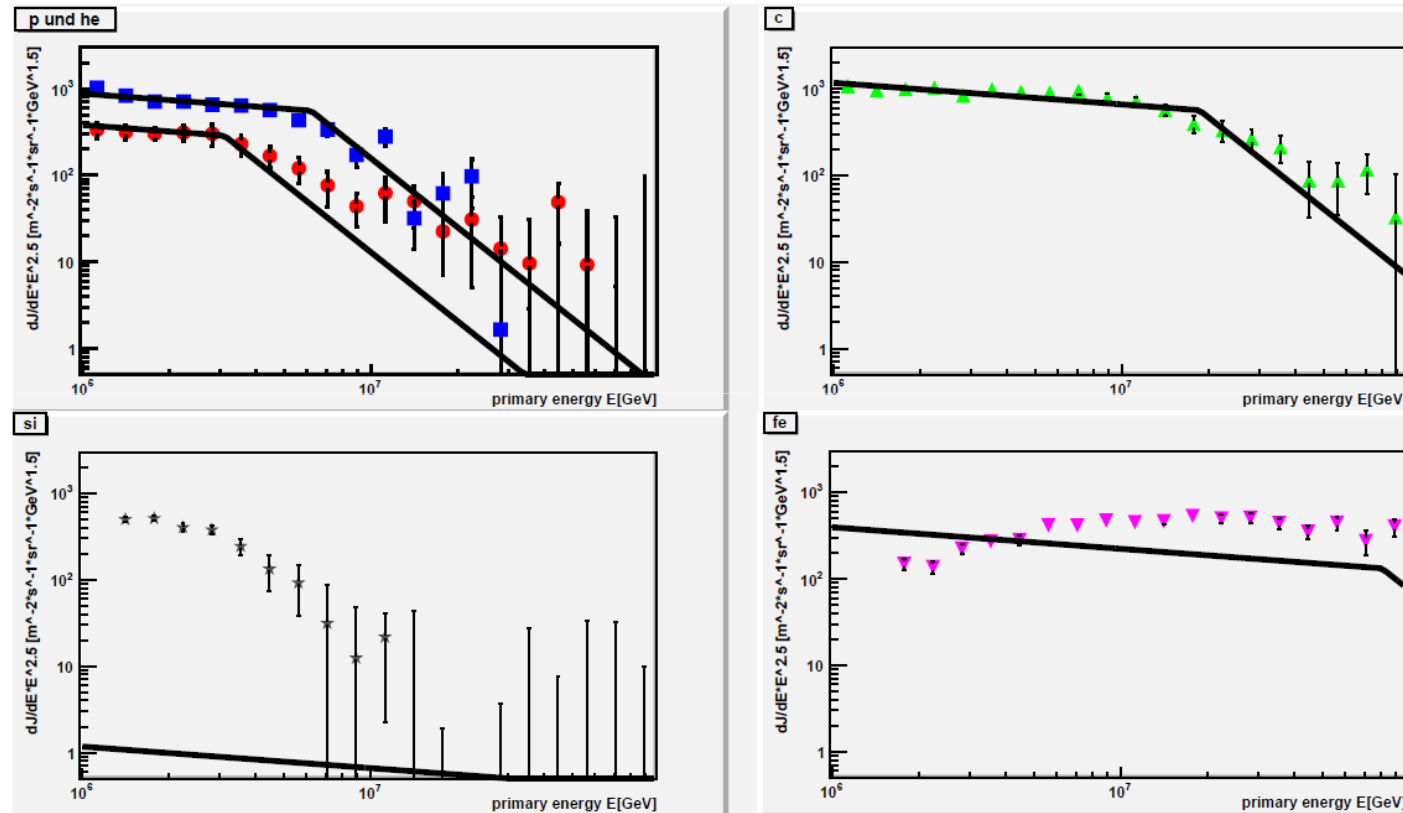
$$[2] = -0.267562 \pm 0.021781$$

$$[3] = -2.28873 \pm 0.134892$$

4. Fit strategies

Improved fit with Minuit : Use iterations

SYBILL



$$[1] = 3.10114e+06 \text{ GeV} \pm 109758 \text{ GeV}$$

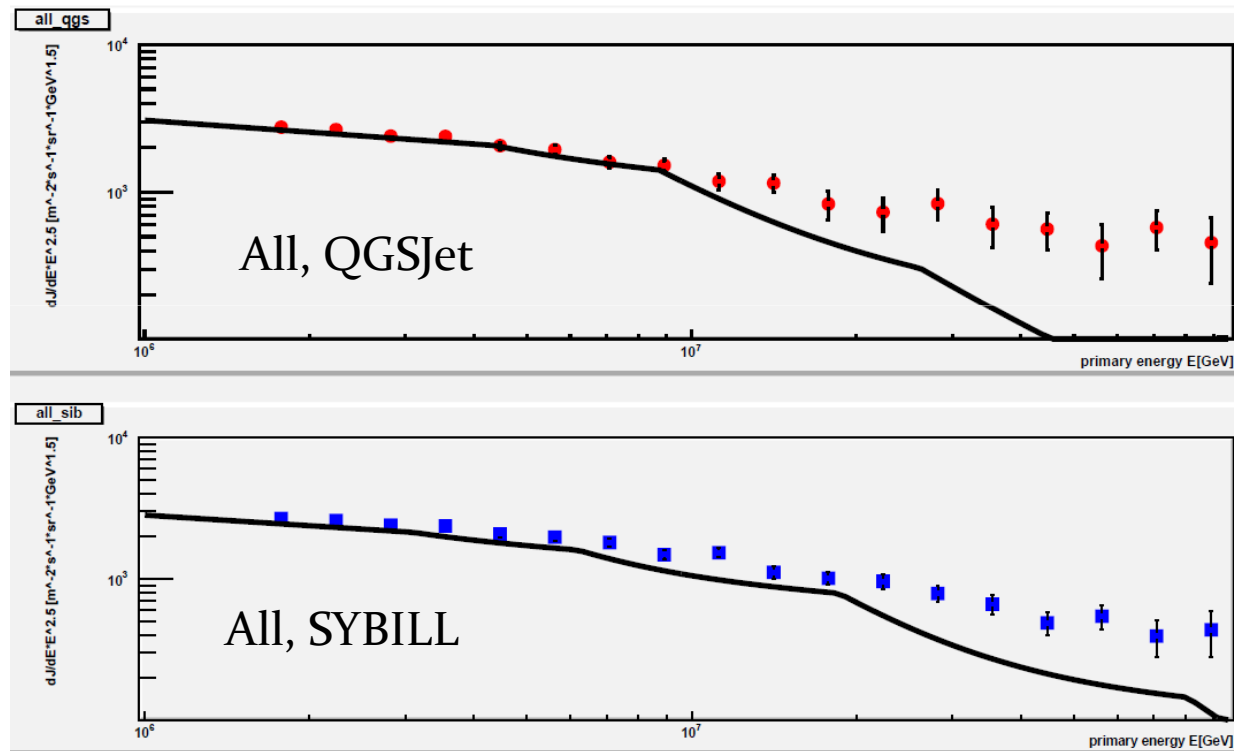
$$[2] = -0.249798 \pm 0.018478$$

$$[3] = -2.64861 \pm 0.150964$$

4. Fit strategies

Improved fit with Minuit : Use iterations

Plot sum of fit functions into all-particle spectra:

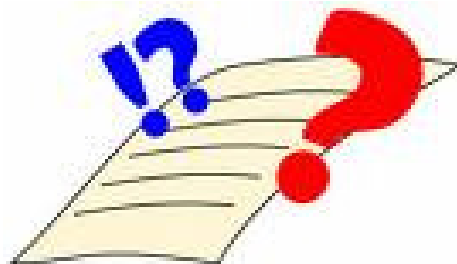


- Silicon iron is missing! -> Improvement by „eliminating“ data
- Is there an technical error?

5. Summary & Outlook

- Atmospheric μ - and ν -Fluxes are background for extragalactic ν , μ and therefore must be known
- They can be calculated with CORSIKA by using parameters which describe spectra of mass groups
- Used fit method has to be improved furthermore, but in principle fluxes can be calculated now
- In near future further questions can be analysed , e.g.:

„Are Neutrino telescopes able to make a statement about the composition of CR with measured fluxes of atmospheric Neutrinos?“





Thank you!!!



Literature

- Several KASCADE people :
„KASCADE measurements of energy spectra for elemental groups of cosmic rays : Results and open problems“ (2004)